

Module 2: Time Value of Money in Finance (Study)

Question 1:

An investor has three options for receiving payments from an investment: Option 1: a single payment of \$136,000 today; Option 2: 30 annual payments of \$12,000, beginning one year from today; Option 3: 20 annual payments of \$13,000, beginning today. If the annual discount rate is 8%, the option with the highest present value is:

A. Option 1.

Incorrect because Option 3 (annuity due with 20 payments of \$13,000 each) has the highest present value of \$137,847. The PV of Option 1 is \$136,000. If a candidate incorrectly calculated the present value of Option 3 as an ordinary annuity, the lump sum of \$136,000 would have the highest present value. Incorrect calculator solution for Option 3: End mode; N = 20; I/Y = 8; PMT = -13,000; compute PV = 127,636.

B. Option 2.

Incorrect because Option 3 (annuity due with 20 payments of \$13,000 each) has the highest present value of \$137,847. The PV of Option 2 is \$135,093. If a candidate ignored the discount rate, the option with the 30 payments of \$12,000 each would have the highest value. That is, Option 2's 30 payments of \$12,000 for a total of \$360,000 is larger than Option 3's 20 payments of \$13,000 for a total of \$260,000 and the lump sum payment of \$136,000.

[CORRECT] C. Option 3.

Correct because Option 3 (annuity due with 20 payments of \$13,000 each) has the highest present value of the annuities and the \$136,000 lump sum. Calculator solution for Option 2: End mode; N = 30; I/Y = 8; PMT = -12,000; compute PV = 135,093. Calculator solution for Option 3: Begin mode; N = 20; I/Y = 8; PMT = -13,000; compute PV = 137,847.

Question 2:

An investor needs to make the following payments to cover college tuition fees, starting 10 years from today:

Annual fee (payable at the beginning of each year)	\$50,000
Number of years of fee payments	4

If the investor's annual discount rate is 3%, the minimum investment amount required today to fund all four years of college tuition is closest to:

A. \$138,294.

Incorrect because the annuity is taken as an ordinary annuity rather than an annuity due, leading to a PV 10 years from today of $PV = \$50,000 \times [1 - 1/(1.03)^4]/0.03 = \$50,000 \times 3.717098 = \$185,855$.

The PV of the annuity today would equal $PV = \$185,855/(1.03)^{10} = \$138,294$. Calculator solution: END mode; N = 4; I/Y = 3%; PMT = 50,000; solve for PV = 185,855. Discounted back 10 years: N = 10; I/Y = 3%; FV = 185,855; solve for PV = 138,294. This is also the result if the PV of the annuity due is discounted back 11 years instead of 10 years: $\$191,431/(1.03)^{11} = \$138,294$. Calculator solution: BEGIN mode; N = 4; I/Y = 3%; PMT = 50,000; solve for PV = 191,431. Discounted back 11 years: N = 11; I/Y = 3%; FV = 191,431; solve for PV = 138,294.

Module 2: Time Value of Money in Finance (Study)

[CORRECT] B. \$142,442.

Correct because the present value (PV) of the annuity due 10 years from today equals $PV = \$50,000 + \$50,000 \times [1 - 1/(1.03)^3]/0.03 = \$50,000 + \$50,000 \times 2.828611 = \$191,431$. The PV of the annuity today equals $PV = \$191,431/(1.03)^{10} = \$142,442$. Calculator solution: BEGIN mode; N = 4; I/Y = 3%; PMT = 50,000; solve for PV = 191,431. Discounted back 10 years: N = 10; I/Y = 3%; FV = 191,431; solve for PV = 142,442. Alternatively, the annuity can be treated as an ordinary annuity, with a PV 9 years from today of $PV = \$50,000 \times [1 - 1/(1.03)^4]/0.03 = \$50,000 \times 3.717098 = \$185,855$. The PV of the annuity today equals $PV = \$185,855/(1.03)^9 = \$142,442$. Calculator solution: END mode; N = 4; I/Y = 3%; PMT = 50,000; solve for PV = 185,855. Discounted back 9 years: N = 9; I/Y = 3%; FV = 185,855; solve for PV = 142,442.

C. \$146,716.

Incorrect because the PV of the annuity due is discounted back 9 years instead of 10 years: $\$191,431/(1.03)^9 = \$146,716$. Calculator solution: BEGIN mode; N = 4; I/Y = 3%; PMT = 50,000; solve for PV = 191,431. Discounted back 9 years: N = 9; I/Y = 3%; FV = 191,431; solve for PV = 146,716. This answer is also closest to the PV of the entire required amount: $\$200,000/(1.03)^{10} = \$148,819$.

Question 3:

An investment requires 10 equal annual payments, starting today, and will pay out a lump sum of \$500,000 15 years from today. If the interest rate is 4% per year compounded annually, the required annual payment is closest to:

[CORRECT] A. \$32,913.

Correct because the present value of the future lump sum payment is $PV = FV(1 + r)^{-n} = \$500,000(1 + 0.04)^{-15} = \$277,632.25$. The 10 annual payments form an annuity due (since the payments start today) whose present value equals the present value of an ordinary annuity with 9 annual payments plus the first payment, i.e. $PV = A + A[1 - 1/(1 + r)^9]/r = A(1 + [1 - 1/(1 + 0.04)^9]/0.04) = 8.4353(A)$. Setting the PV of the cash outflows (the annuity) equal to the PV of the cash inflows (the return in 15 years), we can solve for the annual payment amount; $A = \$277,632.25/8.4353 \approx \$32,913$. Calculator solution: BGN; N = 10; I/Y = 4; PV = 277,632.25; solve for PMT = 32,913.

B. \$34,230.

Incorrect because it mistakes the required payments as an ordinary annuity, rather than an annuity due, calculating their present value as: $PV = A[1 - 1/(1 + r)^n]/r = A([1 - 1/(1 + 0.04)^{10}]/0.04) = 8.1109(A)$. The present value of the return at $t = 15$ is $PV = FV(1 + r)^{-n} = \$500,000(1 + 0.04)^{-15} = \$277,632.25$. Setting these two values equal and solving for the annual payment thus yields: $A = \$277,632.25/8.1109 \approx \$34,230$. Calculator solution: END; N = 10; I/Y = 4; PV = 277,632.25; solve for PMT = 34,230.

C. \$40,044.

Incorrect because it assumes the \$500,000 return is paid at $t = 10$ instead of $t = 15$. The present value of this payment is therefore $PV = FV(1 + r)^{-n} = \$500,000(1 + 0.04)^{-10} = \$337,782.08$. The 10 annual payments form an annuity due (since the payments start today) whose present value equals the present value of an ordinary annuity with 9 annual payments plus the first payment, i.e. $PV = A + A[1 - 1/(1 +$

Module 2: Time Value of Money in Finance (Study)

$r)^n]/r = A(1 + [1 - 1/(1 + 0.04)^9]/0.04) = 8.4353(A)$. Setting the PV of the cash outflows (the annuity) equal to the PV of the cash inflows (the return in 15 years), we can solve for the annual payment amount; $A = \$337,782/8.4353 \approx \$40,044$. Calculator solution: BGN; N = 10; I/Y = 4; FV = 500,000; solve for PMT = 40,044.

Question 4:

An investment pays \$1,000 annually for five years, with the first payment occurring three years from today. If the discount rate is 6% compounded annually, the present value of the investment today is closest to:

A. \$3,537.

Incorrect because it recognizes the investment as a delayed annuity, but it wrongly assumes that the first annuity payment for an ordinary annuity starts at $t = 4$ instead of $t = 3$. Thus, it computes the present value of an ordinary annuity at $t = 3$ as $PV = A[1 - 1/(1 + r)^n] / r = \$1,000 \times [1 - 1/(1 + 0.06)^5] / 0.06 = \$4,212.36$. Using the present value formula for a lump sum to bring the single cash flow from $t = 3$ to $t = 0$, $PV = FV(1 + r)^{-n} = \$4,212.36 (1 + 0.06)^{-3} = \$3,536.78 \sim \$3,537$. Calculator solution: (1) END mode; N = 5; I = 6%; PMT = -1,000; FV = 0; solve for PV = 4,212.36. (1) END mode; N = 3; I = 6%; PMT = 0; FV = 4,212.36; solve for PV = 3,536.78 $\sim$ 3,537.

[CORRECT] B. \$3,749.

Correct because by drawing a timeline, the investment is recognized as a delayed annuity with the first payment starting at $t = 3$. The first step is to compute the present value of an ordinary annuity at $t = 2$ because the first annuity payment is then one period away, as $PV = A[1 - 1/(1 + r)^n] / r = \$1,000 \times [1 - 1/(1 + 0.06)^5]/0.06 = \$4,212.36$. Using the present value formula for a lump sum to bring the single cash flow from $t = 2$ to $t = 0$, $PV = FV(1 + r)^{-n} = \$4,212.36 (1 + 0.06)^{-2} = \$3,748.99 \sim \$3,749$. Calculator solution: (1) END mode; N = 5; I = 6%; PMT = -1,000; FV = 0; solve for PV = 4,212.36. (2) END mode; N = 2; I = 6%; PMT = 0; FV = 4,212.36; solve for PV = 3,748.99 $\sim$ 3,749. A second method to compute the present value of the investment is to recognize it as an annuity due with first payment at $t = 3$, and then discount back three periods using the present value formula for a lump sum. $PV = \{A[1 - 1/(1 + r)^n] / r\}(1 + r) = \$1,000 \times \{[1 - 1/(1 + 0.06)^5]/0.06\} \times (1 + 0.06) = \$4,465.11$. Using the present value formula for a lump sum to bring the single cash flow from $t = 3$ to $t = 0$, $PV = FV(1 + r)^{-n} = \$4,465.11 (1 + 0.06)^{-3} = \$3,748.99 \sim \$3,749$. Calculator solution: (1) BGN mode; N = 5; I = 6%; PMT = -1,000; FV = 0; solve for PV = 4,465.11. (2) END mode; N = 3; I = 6%; PMT = 0; FV = 4,465.11; solve for PV = 3,748.99 $\sim$ 3,749. Another method to compute the correct answer is to calculate the present value of a series of equal cash flows, with the first cash flow in the third year. Using a calculator with CF=0, CF=0, CF=1000, CF=1000, CF=1000, CF=1000, CF=1000; I=6%; solve for NPV= 3,748.99 $\sim$ 3,749.

C. \$4,212.

Incorrect because it is the present value of the investment as $t = 2$ instead of $t = 0$, and it is an intermediate step in the correct calculation. It computes present value of an ordinary annuity at $t = 3$ as $PV = A[1 - 1/(1 + r)^n] / r = \$1,000 \times [1 - 1/(1 + 0.06)^5] / 0.06 = \$4,212.36$. Calculator solution: END mode; N = 5; I = 6%; PMT = -1,000; FV = 0; solve for PV = 4,212.36 $\sim$ 4,212.

Module 2: Time Value of Money in Finance (Study)

Question 5:

Grupo Ignacia issued 10-year corporate bonds two years ago. The bonds pay an annualized coupon of 10.7 percent on a semiannual basis, and the current annualized YTM is 11.6 percent. The current price of Grupo Ignacia's bonds (per MXN100 of par value) is closest to:

A. MXN95.47.

B. MXN97.18.

[CORRECT] C. MXN95.39.

Explanation:

C is correct. The coupon payments are 5.35 ($=10.7/2$), the discount rate is 5.8 percent ($=11.6\%/2$) per period, and the number of periods is 16 ($=8 \times 2$). Using Equation 6, the calculation is as follows: $95.39 = 5.35 \cdot 1.058 + 5.35 \cdot 1.058^2 + 5.35 \cdot 1.058^3 + 5.35 \cdot 1.058^4 + \dots + 5.35 \cdot 1.058^{14} + 5.35 \cdot 1.058^{15} + 105.35 \cdot 1.058^{16}$. Alternatively, using the Microsoft Excel or Google Sheets PV function (PV (0.058,16,5.35,100,0)) also yields a result of MXN95.39. A is incorrect. MXN95.47 is the result when incorrectly using coupon payments of 10.7, a discount rate of 11.6 percent, and 8 as the number of periods. B is incorrect. MXN97.18 is the result when using the correct semiannual coupons and discount rate, but incorrectly using 8 as the number of periods.

Question 6:

Grey Pebble Real Estate seeks a fully amortizing fixed-rate five-year mortgage loan to finance 75 percent of the purchase price of a residential building that costs NZD5 million. The annual mortgage rate is 4.8 percent. The monthly payment for this mortgage would be closest to:

[CORRECT] A. NZD70,424.

B. NZD93,899.

C. NZD71,781.

Explanation:

A is correct. The present value of the mortgage is NZD3.75 million ($=0.75 \times 5,000,000$), the periodic discount rate is 0.004 ($=0.048/12$), and the number of periods is 60 ($=5 \times 12$). Using Equation 8, $A = \$70,424 = 0.4\% \text{ (NZD } 3,750,000) \cdot 1 - (1 + 0.4\%)^{-60}$. Alternatively, the spreadsheet PMT function may be used with the inputs stated earlier. B is incorrect. NZD93,899 is the result if NZD5 million is incorrectly used as the present value term. C is incorrect. NZD71,781 is the result if the calculation is made using 4.8 percent as the rate and 5 as the number of periods, then the answer is divided by 12.

Question 7:

Mylandia Corporation pays an annual dividend to its shareholders, and its most recent payment was CAD2.40. Analysts following Mylandia expect the company's dividend to grow at a constant rate of 3 percent per year in perpetuity. Mylandia shareholders require a return of 8 percent per year. The expected share price of Mylandia is closest to:

Module 2: Time Value of Money in Finance (Study)

A. CAD48.00.

[CORRECT] B. CAD49.44.

C. CAD51.84.

Explanation:

B is correct. Mylandia's next expected dividend is CAD2.472 ($=2.40 \times 1.03$), and using Equation 14, $PV = 2.40 (1 + 0.03)^{-1} = 2.33097$. The expected share price of Mylandia stock is:

Question 8:

Suppose Mylandia announces that it expects significant cash flow growth over the next three years, and now plans to increase its recent CAD2.40 dividend by 10 percent in each of the next three years. Following the 10 percent growth period, Mylandia is expected to grow its annual dividend by a constant 3 percent indefinitely. Mylandia's required return is 8 percent. Based upon these revised expectations, The expected share price of Mylandia stock is:

A. CAD49.98.

B. CAD55.84.

[CORRECT] C. CAD59.71.

Explanation:

C is correct. Following the first step, we observe the following expected dividends for Mylandia for the next three years: In 1 year: $D = CAD2.64 (=2.40 \times 1.10)$ In 2 years: $D = CAD2.90 (=2.40 \times 1.10^2)$ In 3 years: $D = CAD3.19 (=2.40 \times 1.10^3)$ The second step involves a lower 3 percent growth rate. At the end of year four, Mylandia's dividend (D) is expected to be $CAD3.29 (=2.40 \times 1.10^3 \times 1.03)$. At this time, Mylandia's expected terminal value at the end of three years is CAD65.80 using Equation 17, as follows: $E(S) = 3.29 / (0.08 - 0.03) = 65.80$. Third, we calculate the sum of the present values of these expected dividends using Equation 16: $PV = 2.64 / 1.08 + 2.90 / 1.08^2 + 3.19 / 1.08^3 + 65.80 / 1.08^3 = 59.71$.

Question 9:

Consider a Swiss Confederation zero-coupon bond with a par value of CHF100, a remaining time to maturity of 12 years and a price of CHF89. In three years' time, the bond is expected to have a price of CHF95.25. If purchased today, the bond's expected annualized return is closest to:

A. 0.58 percent.

B. 1.64 percent.

[CORRECT] C. 2.29 percent.

Explanation:

C is correct. The FV of the bond is CHF95.25, the PV is CHF89, and the number of annual periods (t) is 3. Using Equation 18, $2.29 \text{ percent} = (95.25/89)^{1/3} - 1$. A is incorrect as the result is derived using t of 12. B is incorrect as this result is derived using a PV of CHF95.25 and an FV of 100.

Module 2: Time Value of Money in Finance (Study)

Question 10:

Grupo Ignacia issued 10-year corporate bonds four years ago. The bonds pay an annualized coupon of 10.7 percent on a semiannual basis, and the current price of the bonds is MXN97.50 per MXN100 of par value. The YTM of the bonds is closest to:

[CORRECT] A. 11.28 percent.

B. 11.50 percent.

C. 11.71 percent.

Explanation:

A is correct. The YTM is calculated by solving for the RATE spreadsheet function with the following inputs: number of periods of 12 ($=6 \times 2$), coupon payments of 5.35 ($=10.7/2$), PV of -97.50, and FV of 100. The resulting solution for RATE of 5.64 percent is in semiannual terms, so multiply by 2 to calculate annualized YTM of 11.28 percent. B is incorrect, as 11.50 percent is the result if number of periods used is eight, instead of 12. C is incorrect, as 11.71 percent is the result if the number of periods used is 6, instead of 12.

Question 11:

Mylandia Corporation stock trades at CAD60.00. The company pays an annual dividend to its shareholders, and its most recent payment of CAD2.40 occurred yesterday. Analysts following Mylandia expect the company's dividend to grow at a constant rate of 3 percent per year. Mylandia's required return is:

A. 8.00 percent.

B. 7.00 percent.

[CORRECT] C. 7.12 percent.

Explanation:

C is correct. We may solve for required return based upon the assumption of constant dividend growth using Equation 21: $r = \frac{2.40 (1.03)}{60} + 0.03 = 0.0712$. B is incorrect as 7.00 percent is the result if we use the previous dividend of CAD2.40 instead of the next expected dividend. A is incorrect as 8.00 percent is simply the required return assumed from one of the Mylandia examples in Question Set 1 in which the price is solved to be a lower value.

Question 12:

An analyst observes the benchmark Indian NIFTY 50 stock index trading at a forward price-to-earnings ratio of 15. The index's expected dividend payout ratio in the next year is 50 percent, and the index's required return is 7.50 percent. If the analyst believes that the NIFTY 50 index dividends will grow at a constant rate of 4.50 percent in the future, which of the following statements is correct?

A. The analyst should view the NIFTY 50 as overpriced.

[CORRECT] B. The analyst should view the NIFTY 50 as underpriced.

C. The analyst should view the NIFTY 50 as fairly priced.

Module 2: Time Value of Money in Finance (Study)

Explanation:

B is correct. Using Equation 24, the previous input results in the following inequality: $15 < 0.50 \cdot 0.075 - 0.045 = 16.67$. The above inequality implies that the analyst should view the NIFTY 50 as priced too low. The fundamental inputs into the equation imply a forward price to earnings ratio of 16.67 rather than 15. An alternative approach to answering the question would be to solve for implied growth using the observed forward price to earnings ratio of 15 and compare this to the analyst's growth expectations: $15 = 0.50 \cdot 0.075 - g$. Solving for g yields a result of 4.1667 percent. Since the analyst expects higher NIFTY 50 dividend growth of 4.50 percent, the index is viewed as underpriced.

Question 13:

If you require an 8 percent return and must invest USD500,000, which of the investment opportunities in Exhibit 1 should you prefer?

Exhibit 1 Investment Opportunities

Cash flows (in thousands)	t = 0	t = 1	t = 2	t = 3
Opportunity 1	-500	195	195	195
Opportunity 2	-500	225	195	160.008

A. Opportunity 1

B. Opportunity 2

[CORRECT] C. Indifferent between the two opportunities.

Explanation:

C is correct. Using cash flow additivity, compare the two opportunities by subtracting Opportunity 2 from Opportunity 1 yielding the following cash flows:

Opportunity 1 - Opportunity 2	0	-30	0	34.992
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Finding the present value of the above cash flows at 8 percent discount rate shows that both investment opportunities have the same present value. Thus, the two opportunities are economically identical, and there is no clear preference for one over the other.

Question 14:

Italian one-year government debt has an interest rate of 0.73 percent; Italian two-year government debt has an interest rate of 1.29 percent. The breakeven one-year reinvestment rate, one year from now is closest to:

A. 1.01 percent.

B. 1.11 percent.

[CORRECT] C. 1.85 percent.

Module 2: Time Value of Money in Finance (Study)

Explanation:

C is correct. The one-year forward rate reflects the breakeven one-year reinvestment rate in one year, computed as follows: $F_{1,2} = (1+r_1)^2 / (1+r_2) - 1$, $F_{1,2} = (1.0129)^2 / (1.0073) - 1 = 0.0185$.

Question 15:

The current exchange rate between the euro and US dollar is USD/EUR1.025. Risk-free interest rates for one year are 0.75 percent for the euro and 3.25 percent for the US dollar. The one-year USD/EUR forward rate that best prevents arbitrage opportunities is:

[CORRECT] A. USD/EUR1.051.

B. USD/EUR1.025.

C. USD/EUR0.975.

Explanation:

A is correct. To avoid arbitrage opportunities in exchanging euros and US dollars, investors must be able to lock in a one-year forward exchange rate of USD/EUR1.051 today. The solution methodology is shown below. In one year, a single unit of euro invested risk-free is worth EUR1.0075 ($=e^{0.0075}$). In one year, a single unit of euro converted to US dollars and then invested risk-free is worth USD1.0589 ($=1.025 \times e^{0.0325}$). To convert USD1.0589 into EUR1.0075 requires a forward exchange rate of USD/EUR1.051 ($=1.0589/1.0075$).

Question 16:

A stock currently trades at USD25. In one year, it will either increase in value to USD35 or decrease to USD15. An investor sells a call option on the stock, granting the buyer the right, but not the obligation, to buy the stock at USD25 in one year. At the same time, the investor buys 0.5 units of the stock. Which of the following statements about the value of the investor's portfolio at the end of one year is correct?

[CORRECT] A. The portfolio has a value of USD7.50 in both scenarios.

B. The portfolio has a value of USD25 in both scenarios.

C. The portfolio has a value of USD17.50 if the stock goes up and USD7.50 if the stock goes down.

Explanation:

A is correct. Regardless of whether the stock increases or decreases in price, the investor's portfolio has a value of USD7.50 as follows: If stock price goes to USD35, value = $0.5 \times 35 - 10 = 7.50$. If stock price goes to USD15, value = $0.5 \times 15 - 0 = 7.50$. If the stock price rises to USD35, the sold call option at USD25 has a value to the buyer of USD10, offsetting the rise in the stock price.

Module 2: Time Value of Money in Finance (Study)

Question 17:

A consultant starts a project today that will last for three years. Her compensation package includes the following:

Year	End-of-Year Payment
1	\$100,000
2	\$150,000
3	\$200,000

If she expects to invest these amounts at an annual interest rate of 3%, compounded annually until her retirement 10 years from now, the value at the end of 10 years is closest to:

A. \$460,590.

Incorrect. It is the sum of the future values of the three cash flows at the end of year three: $\$100,000 \times (1.03)^2 + \$150,000 \times 1.03 + \$200,000 = \$106,090 + \$154,500 + \$200,000 = \$460,590$.

[CORRECT] B. \$566,466.

Correct. First calculate the present value of the three cash flows with the following formula: $PV = FV / (1 + r)^n$. We obtain: $PV_{ca\ fow} = (\$100,000 / 1.03) = \$97,087$ (rounded) $PV_{ca\ fow} = [\$150,000 / (1.03)^2] = \$141,389$ (rounded) $PV_{ca\ fow} = [\$200,000 / (1.03)^3] = \$183,028$ (rounded). Then, sum the three present values: $\$97,087 + \$141,389 + \$183,028 = \$421,504$. Calculate the FV of \$421,504 ten years from now with the formula: $FV = PV \times (1 + r)^n$. $FV = PV \times (1 + r)^{10}$. $FV = \$421,504 \times (1.03)^{10} = \$566,466$ (rounded). The future value 10 years from now is \$566,466. Alternatively, calculate directly the FV of each of the cash flows to the end of 10 years: $FV = \$100,000 \times (1.03)^9 + \$150,000 \times (1.03)^8 + \$200,000 \times (1.03)^7 = \$130,477 + \$190,016 + \$245,975 = \$566,468$ (rounded).

C. \$618,994.

Incorrect. First calculate the future values of the three cash flows at the end of year three: $\$100,000 \times (1.03)^2 + \$150,000 \times 1.03 + \$200,000 = \$106,090 + \$154,500 + \$200,000 = \$460,590$. Then, calculate the FV of \$460,590 at the end of year 13: $\$460,590 \times (1.03)^{10} = \$618,994$.

Question 18:

A consumer purchases an automobile using a loan. The amount borrowed is €30,000, and the terms of the loan call for the loan to be repaid over five years using equal monthly payments with an annual nominal interest rate of 8% and monthly compounding. The monthly payment is closest to:

[CORRECT] A. €608.29.

Correct. Using a financial calculator: $N = 60$, $I/Y = 8/12$, $PV = 30,000$, $FV = 0$, and compute PMT. Note, 5 years = 60 months. The nominal rate of 8% must be divided by 12 to find the monthly periodic rate of 0.6666667%. Alternatively, using the present value of an annuity formula, solve: $PV = A [1 - 1 / (1 + (r / m))^n] / (r / m)$. $30,000 = A [1 - 1 / (1 + 0.08 / 12)^{60}] / (0.08 / 12)$. $30,000 = A \times 49.318433$. $A = 30,000 / 49.318433 = 608.291829$.

Module 2: Time Value of Money in Finance (Study)

B. €626.14.

Incorrect. It uses $N = 5$, $I/Y = 8$, $PV = 30,000$, $FV = 0$, compute $PMT = 7513.69$. $7,513.69/12 = 626.14$.

C. €700.00.

Incorrect. It is calculated using: $\text{Interest} = €30,000 \times 0.08 \times 5 = €12,000$; $\text{Payment} = (€30,000 + €12,000)/60 = €700$

Question 19:

A financial contract offers to pay €1,200 per month for five years with the first payment made immediately. Assuming an annual discount rate of 6.5%, compounded monthly, the present value of the contract is closest to:

A. €61,330.

Incorrect. This is the PV of a 60-month ordinary annuity. $N = 60$, the discount rate (I/Y) = $6.5/12$; $PMT = 1,200$, $FV = 0$. Mode = End; Calculate PV: $PV = 61,330.41$.

[CORRECT] B. €61,663.

Correct. Using a financial calculator: $N = 60$; the discount rate (I/Y) = $(6.5\%/12) = 0.54166667$; $PMT = €1,200$; Future value = €0; Mode = Begin; Calculate present value (PV): $PV = €61,662.62$. Alternatively: Treat the stream as an ordinary annuity of 59 periods and add the current value of €1,200 to the derived answer. Using a financial calculator: $N = 59$; the discount rate (I/Y) = $(6.5\%/12) = 0.54166667$; $PMT = €1,200$; Future value = €0; Mode = End; Calculate PV: $PV = €60,462.62$; Total PV = $€1,200 + €60,462.62 = €61,662.62$.

C. €63,731.

Incorrect. This is the PV of an annuity due of 5 periods, 6.5% interest, and payments of 14,400 ($1,200 \times 12$): $N = 5$; the discount rate (I/Y) = 6.5; $PMT = 14,400$; $FV = 0$; Mode = Begin; Calculate PV = 63,731.49.

Question 20:

An individual wants to be able to spend €80,000 per year for an anticipated 25 years in retirement. To fund this retirement account, he will make annual deposits of €6,608 at the end of each of his working years. He can earn 6% compounded annually on all investments. The minimum number of deposits that are needed to reach his retirement goal is closest to:

A. 28.

Incorrect. 80,000 is multiplied by 25 years and then discounted at 6% for 25 years (465,997). The result is used as the PV of the 6,608 annuity at 6% as follows: $I/Y = 6\%$; $PMT = 6,608$; $PV = 465,997$; $FV = 0$; Calculate N: $N = -28.40$ and the minus sign is ignored.

[CORRECT] B. 40.

Correct. The following figure represents the timeline for the problem: Expand / Collapse
Extended Description The first tick is zero. The second is 1 open bracket 6 6 0 8 euro close bracket. There are three ellipses denoting a large gap. The third is italic capital R open bracket 6 6 0 8 euro close bracket.

Module 2: Time Value of Money in Finance (Study)

The fourth is italic capital R plus 1 open bracket 80 thousand euro close bracket. There are three ellipses denoting a large gap. The fifth is italic capital R plus 25 open bracket 80 thousand euro close bracket. Using a financial calculator, the funds needed at retirement (R on the timeline) are calculated: $N = 25$; $I/Y = 6\%$; $PMT = €80,000$; Future value (FV) = €0; Mode = End. The calculated present value (PV) is €1,022,668. $PV = A [1 - 1 / (1 + r)^n] / r = 80,000 [1 - 1 / (1.06)^{25}] / 0.06 = 1,022,668$ Then, €1,022,668 is used as the FV (at R on the timeline) for the accumulation phase annuity as per: $I/Y = 6\%$; $PV = €0$; $PMT = -€6,608$; $FV = €1,022,668$; Mode = End. The computed N is 40. Alternatively, 40 could be calculated with the formula: $FV = A [(1 + r)^n - 1] / r$ and solving for N, $1,022,668 = 6,608 [(1 + 0.06)^n - 1] / 0.06$

C. 51.

Incorrect. 80,000 is multiplied by 25 years (2,000,000) and the result is used as the FV of the 6,608 annuity at 6% and $PV = 0$. The result is $N = 50.67$.

Question 21:

An annuity makes seven annual payments of \$10,000 each, with the first payment occurring five years from today. If the discount rate is 6% per year, the value of the annuity today is closest to:

A. \$41,715.

Incorrect because it assumes the ordinary annuity starts in Year 5 instead of Year 4. The present value of an ordinary annuity with 7 payments of \$10,000 at a 6% discount rate is calculated as follows: $PV = A [1 - 1 / (1 + r)^n] / r$ $PV = \$10,000 \times [1 - 1 / (1 + 0.06)^7] / 0.06$ $PV = \$55,823.81$ Then the PV of the investment is incorrectly discounted from Year 5 instead of Year 4 such that: $PV = FV (1 + r)^{-n}$ $PV = \$55,823.81 \times (1 + 0.06)^{-5}$ $PV = \$41,714.80 \approx \$41,715$. Calculator solution: (1) END mode; $N = 7$; $I = 6$; $PMT = -10,000$; $FV = 0$; solve for $PV = 55,823.81$. (2) END mode; $N = 5$; $I = 6$; $PMT = 0$; $FV = -55,823.81$; solve for $PV = 41,714.80$.

[CORRECT] B. \$44,218.

Correct because the present value in Year 4 of an ordinary annuity with 7 payments of \$10,000 at a 6% discount rate is calculated as follows: $PV = A [1 - 1 / (1 + r)^n] / r$ $PV = \$10,000 \times [1 - 1 / (1 + 0.06)^7] / 0.06$ $PV = \$55,823.81$ Then, using a time line, the PV of the annuity in today's dollars is $PV = FV (1 + r)^{-n}$ $PV = \$55,823.81 \times (1 + 0.06)^{-4}$ $PV = \$44,217.69 \approx \$44,218$. Calculator solution: (1) END mode; $N = 7$; $I = 6$; $PMT = -10,000$; $FV = 0$; solve for $PV = 55,823.81$. (2) END mode; $N = 4$; $I = 6$; $PMT = 0$; $FV = -55,823.81$; solve for $PV = 44,217.69$.

C. \$55,824.

Incorrect because it is an intermediate step in the calculation and it represents the value of the annuity in 4 years. The present value in Year 4 of an ordinary annuity with 7 payments of \$10,000 at a 6% discount rate is calculated as follows: $PV = A [1 - 1 / (1 + r)^n] / r$ $PV = \$10,000 \times [1 - 1 / (1 + 0.06)^7] / 0.06$ $PV = \$55,823.81 \approx \$55,824$. Calculator solution: (1) END mode; $N = 7$; $I = 6$; $PMT = -10,000$; $FV = 0$; solve for $PV = 55,823.81$.